



COURSE: DESIGN OF CONCRETE STRUCTURE-I

TOPIC: DESIGN OF COLUMN BY LSM

LECTURE: 06

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⇒ Design of Column subjected to Axial load + Uniaxial Bending

If a column is to be designed for

(i) Axial load =  $P_U$

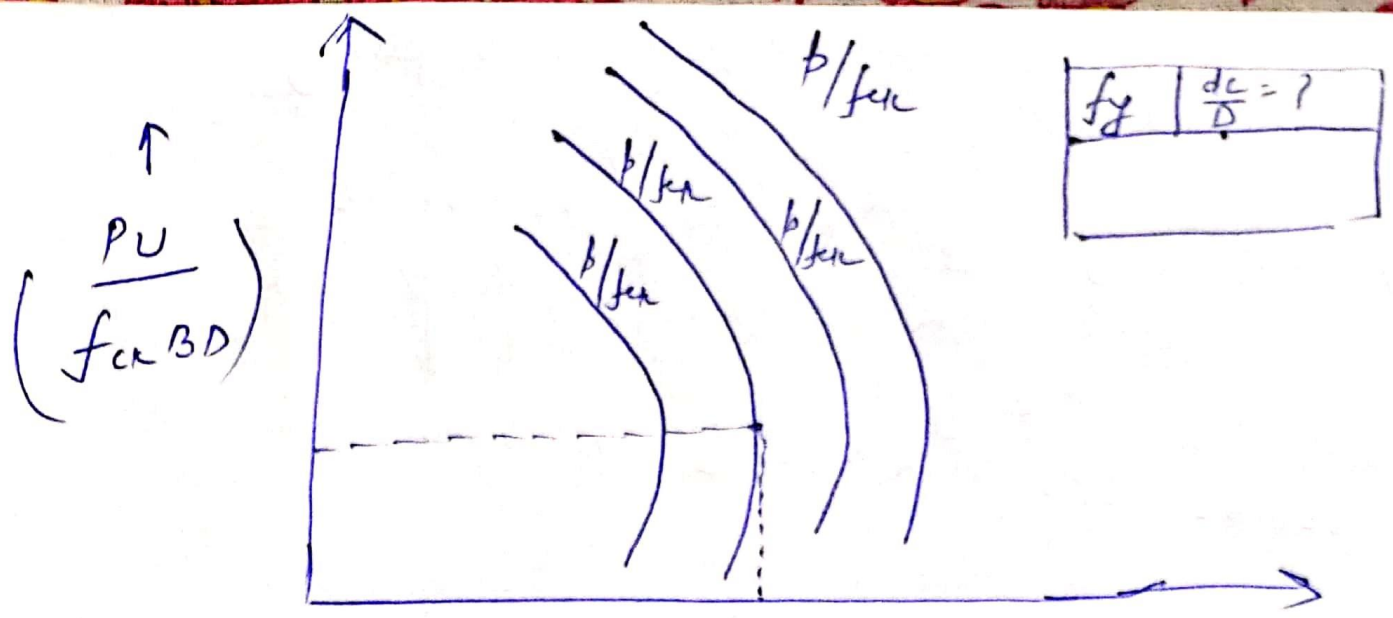
(ii) Moment =  $M_U$

$$[M_U \text{ \& } M_{Umin}]$$

$$M_{Umin} = P_U \times e_{min}$$

→ Interaction diagram are used as per SP-16 (Design Aids for Reinforced Concrete : IS 456 : 1978)

Interaction Curve: A/c to IS 456 : 1978 (SP-16)  
It is the curve b/w Non dimensional load  $\left(\frac{P_U}{f_{ck} B D^2}\right)$  on the y-axis and Non dimensional moment on the x-axis  $\left(\frac{M_U}{f_{ck} B D^2}\right)$



$$\left( \frac{MU}{f_{cc} B D^2} \right) \rightarrow$$

In SP:16 Chart 27 to chart 82)

Non dimensional moment =  $\frac{MU}{f_{cc} B D^2}$

- where  $MU \rightarrow$  factored Bending moment
- $f_{cc} \rightarrow$  characteristic compressive strength of concrete at 28 days
- $B \rightarrow$  width of the column
- $D \rightarrow$  Gross/total depth of column

Non-dimensional load  $\rightarrow \left( \frac{PU}{f_{cc} B D} \right)$

$PU \rightarrow$  factored Axial load.

(03)

With the help of  $\left(\frac{P_u}{f_{ck}BD}\right)$  and  $\left(\frac{M_u}{f_{ck}BD^2}\right)$ , Grade of steel ( $f_y$ ) and  $\left(\frac{d_c}{D}\right)$  we can select interaction curve (chart 27 to chart 82)

$$\frac{p}{f_{ck}} = k$$

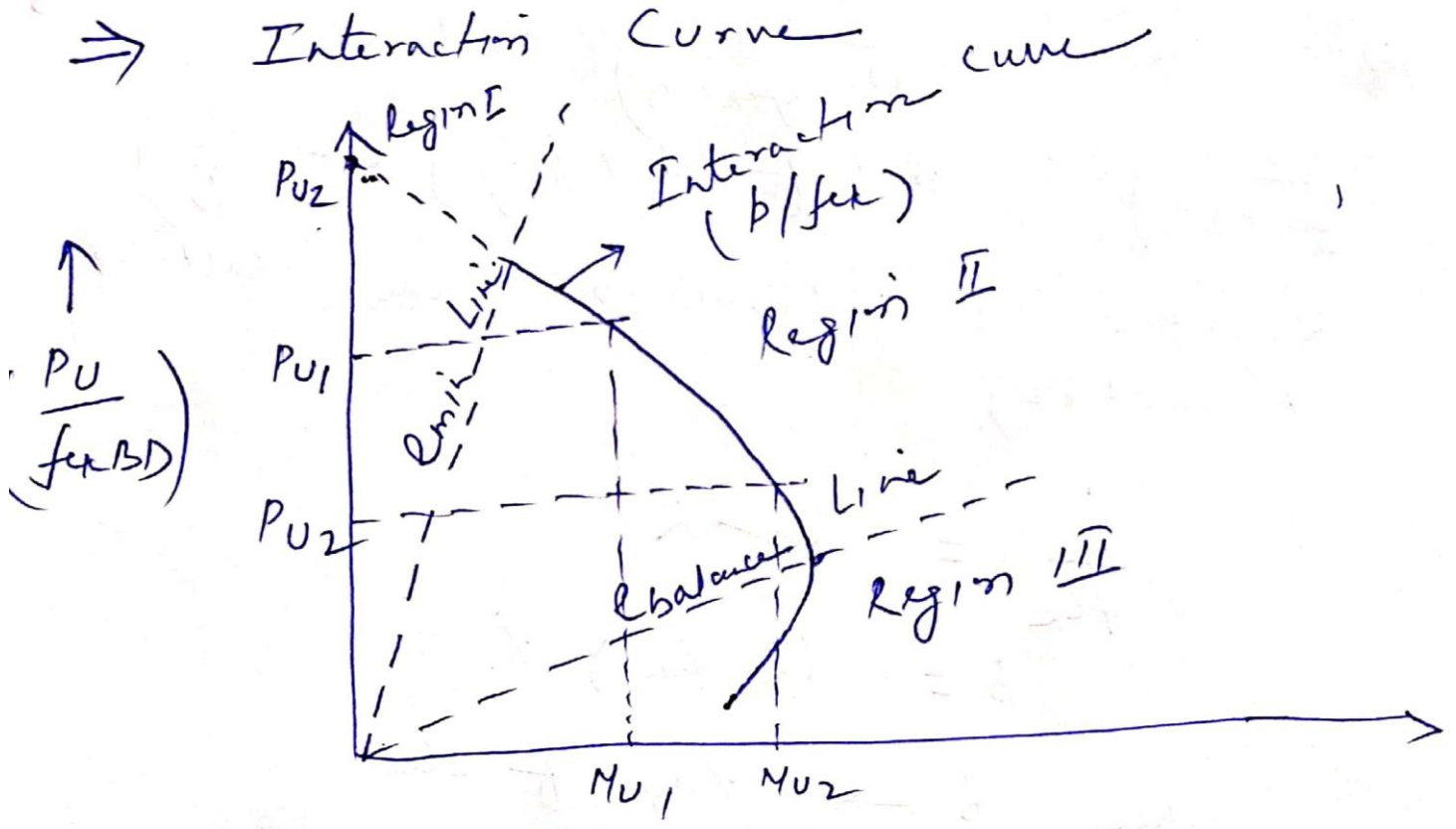
$$p = (k \cdot f_{ck}) \%$$

Where  $p \rightarrow$  % age of steel

$$A_{sc} = \frac{p \times BD}{100}$$

Design of stirrups is same

1. Calculate  $\frac{P_u}{f_{ck}BD} \rightarrow$  y-value
2. Calculate  $\frac{M_u}{f_{ck}BD^2} \rightarrow$  x-value
3. Read the value of  $\frac{p}{f_{ck}} = k$  value  
Get Percentage of steel ( $p$ ) =  $k \cdot f_{ck}$
4. Compute  $A_{sc} = \frac{p \times BD}{100}$
5. Design of stirrups  $\rightarrow$  same



$$\left( \frac{M_u}{f_{ck} B D^2} \right) \rightarrow$$

Region I (Min<sup>m</sup> eccentricity Region)

(When  $e < e_{min}$ )

→ Column can't be designed for this value.

→ 1st point shows  $P_{u2}$  value

$P_{u2}$  → Ultimate load carrying capacity of column.

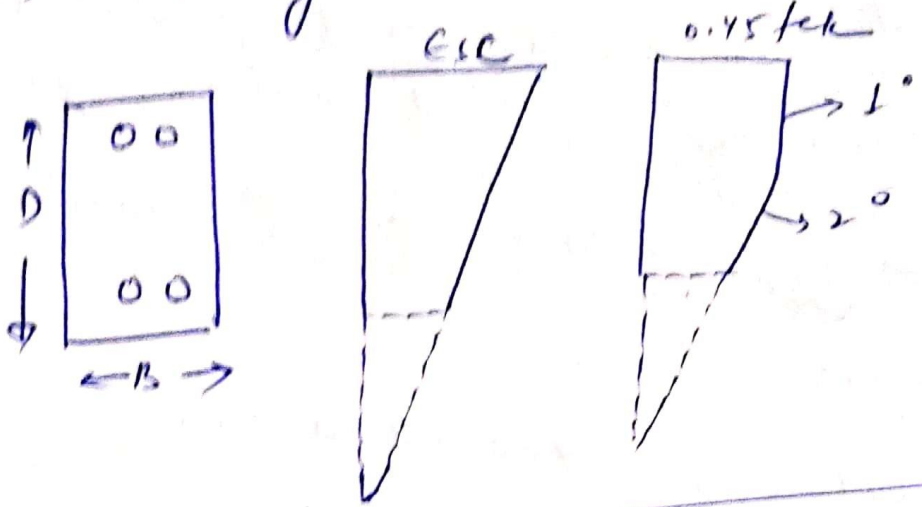
$$P_{u2} = 0.45 f_{ck} A_c + 0.75 f_y A_{sc}$$

②

### Compression Control region

In this region - effect of load & moment both are equally high.

→ Mostly column is in compression.



$$ELC = 0.0035 - 0.75 ELC$$

→ When N.A is formed outside column section if no tension is developed ( $X_u > D$ )

③

### Tension Control region

When load is very less as compared to effect of moment.

→ Tension is developed in the column.

→ Neutral axis will be within the column section ( $X_u < D$ )

→ Maximum strain in concrete = 0.0035.

→ In this region moment carrying capacity get reduced if the load on the column is reduced.

P-1

For a rectangular column of size 400 mm x 400 mm, the value of  $\frac{p}{f_{ck}}$  is taken 0.10 for using interaction curve of column as given in SP-16. The grade of concrete is M20 & the grade of steel is Fe415. The area of steel will be equal to

- (a) 4000 mm<sup>2</sup>
- (b) 3200 mm<sup>2</sup> ←
- (c) 2400 mm<sup>2</sup>
- (d) 1600 mm<sup>2</sup>

Solution

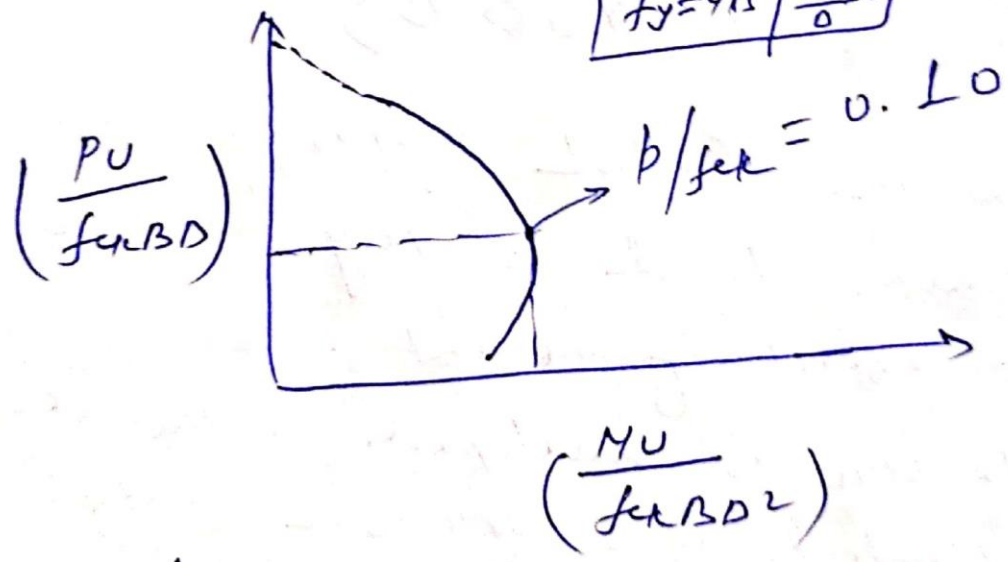
Size of the column = 400 x 400 mm

$$B = 400 \text{ mm}$$

$$D = 400 \text{ mm}$$

For Given  $f_y = 415$  &  $\frac{d_c}{D} = 0$

$f_y = 415$	$\frac{d_c}{D} = 0$
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$$\frac{p}{f_{ck}} = 0.10$$

$$p = 0.10 \times f_{ck} = 0.10 \times 20 = 2$$

$$A_{sc} = \frac{p \times BD}{100} = \frac{2 \times 400 \times 400}{100}$$

$$= 3200 \text{ mm}^2$$

P-2. A rectangular column of size 400x400 mm is loaded with  $P_u = 1200$  kN and  $M_{ux} = 50$  kN-m. For using interaction curve of column, the non-dimensional form of load & Moment will be (M20 grade of concrete)

- Solution
- (a) 0.375 and 0.039 respectively
  - (b) 0.375 and 0.049 respectively
  - (c) 0.469 and 0.039 respectively
  - (d) 0.469 and 0.049 respectively.

Solution

$$B = 400 \text{ mm}$$

$$D = 400 \text{ mm}$$

$$P_u = 1200 \text{ kN}$$

$$M_{ux} = 50 \text{ kN-m}$$

Non-dimensional load  $\left( \frac{P_u}{f_{ck}BD} \right) = \frac{1200 \times 10^3}{20 \times 400 \times 400} = 0.375$

Non-dimensional moment  $\left( \frac{M_u}{f_{ck}BD^2} \right) = \frac{50 \times 10^6}{20 \times 400 \times 400^2} = 0.039$

