

**Department of Civil Engineering  
Kathihar Engineering College, Kathihar**

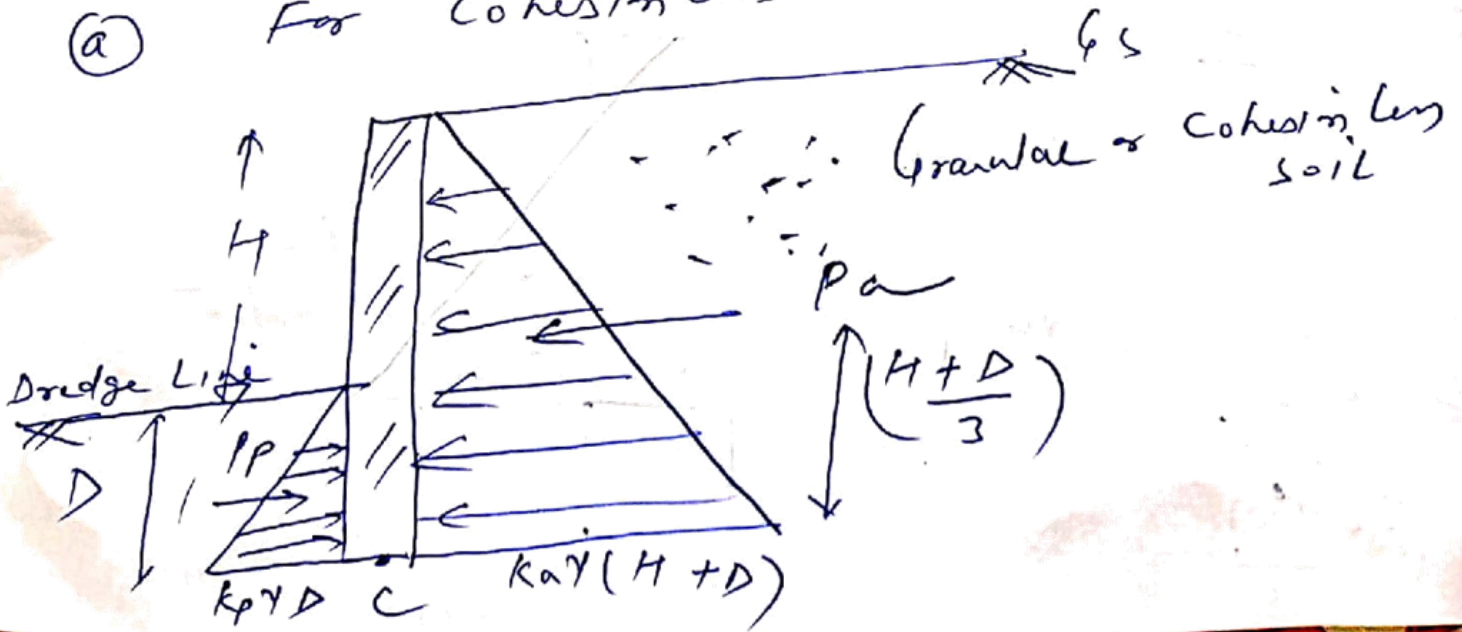
**Subject:** Soil and Rock Mechanics  
**Topic:** Earth Pressure Theory  
**Lecture:** 07  
**Course Instructor:** Prof. Rashid Mustafa

Sheet Pile Wall : Sheet pile consist of number of sheet piles driven side by side to form continuous vertical wall into the medium which is used to retain earth mass.

→ used in water front structure, temporary construction to prevent failure below the gravity dam

TYPES → Cantilever sheet pile  
 Anchored sheet pile

Cantilever sheet pile  
 (a) For cohesionless soil



In order to ensure safety against overturning the min depth of embedment can be calculated as (2)

$$\sum M_c = 0$$

$$P_a \times \left(\frac{H+D}{3}\right) - P_p \times \frac{D}{3} = 0$$

$$\frac{1}{2} k_a \gamma (H+D)^2 \times \left(\frac{H+D}{3}\right) - \frac{1}{2} k_p \gamma D^2 \times \frac{D}{3} = 0$$

$$\frac{1}{2} k_a \gamma \frac{(H+D)^3}{3} = \frac{1}{2} k_p \gamma \frac{D^3}{3}$$

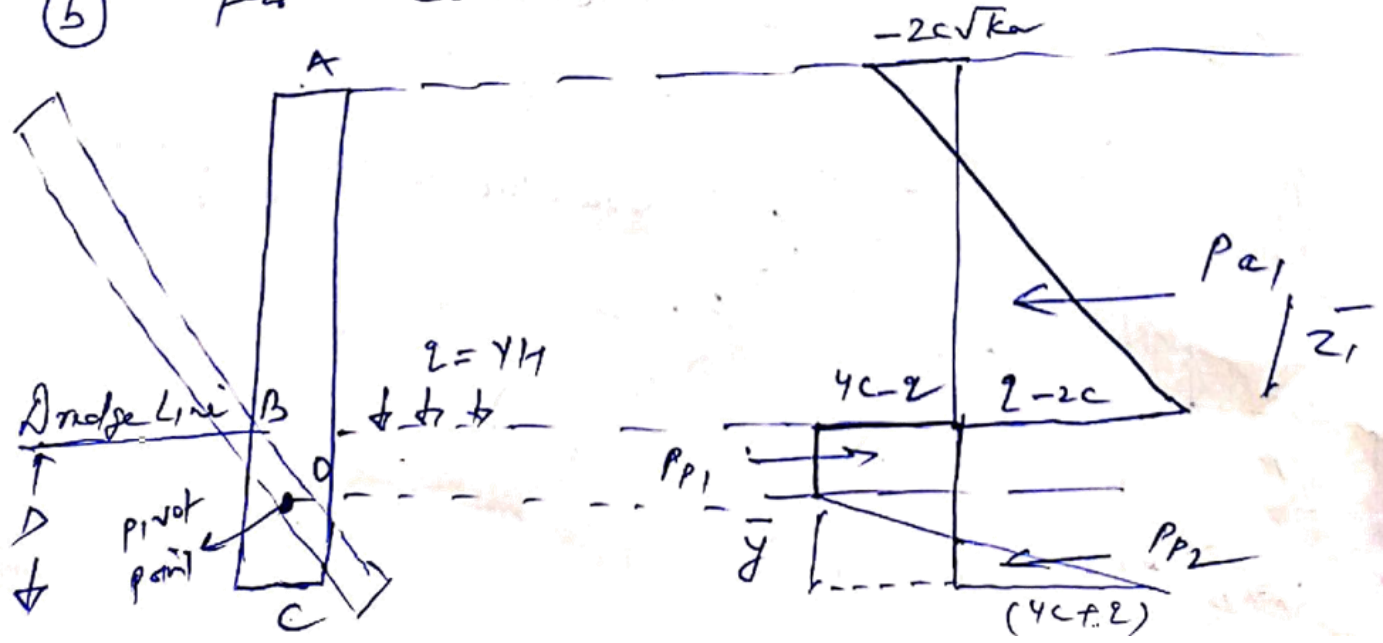
$$k_a (H+D)^3 = k_p (D)^3$$

$$D = \dots$$

If factor of safety is not given then increase D by 30%.

Depth of embedment = 1.3 D

(b) For Cohesive Soil



Above dredge line

Right hand side (Active condition)

$$p_a = k_a \gamma z - 2c\sqrt{k_a}$$

For pure clay ( $\phi=0, k_a=1$ )

$$p_a = \gamma z - 2c$$

At  $z=0$ , Point A,  $p_a = -2c$   
 At  $z=H$ , Point B,  $p_a = \gamma H - 2c$   
 $= \gamma - 2c (\leftarrow)$

At Point B . (Right hand side) Active

$$p_a = \gamma - 2c (\leftarrow)$$

Left hand side (Passive)

$$p_p = k_p \gamma z + 2c\sqrt{k_p} \quad [k_p=1, \sigma_z=0]$$

$$p_p = 2c (\rightarrow)$$

Resultant Earth Pressure

$$p = p_p - (p_a)$$

$$= 2c - (\gamma - 2c) = (4c - \gamma) \rightarrow$$

Below the dredge line at depth  $z$ .

RHS, Active,  $k_a \sigma_v - 2c\sqrt{k_a}$   
 $= k_a (\gamma + \gamma z) - 2c\sqrt{k_a}$

$$p_a = \gamma + \gamma z - 2c (\leftarrow)$$

Resultant Earth Pressure

$$p = p_p - p_a$$

( $\rightarrow$ ) ( $\leftarrow$ )

$$= \gamma z + 2c - (\gamma z - 2c)$$

$$p = (\gamma c - 2c)$$

At the base point C

RHS (Passive)

$$p_p = k_p \sigma_v + 2c\sqrt{k_p}$$
$$= k_p (\gamma d) + 2c\sqrt{k_p}$$
$$= \gamma d + 2c (\leftarrow)$$

LHS Active

$$p_a = k_a \sigma_v - 2c\sqrt{k_a}$$
$$= k_a \gamma d - 2c\sqrt{k_a}$$
$$= \gamma d - 2c (\rightarrow)$$

Resultant Earth Pressure

$$p = p_p - p_a$$
$$= (\gamma d + 2c) - (\gamma d - 2c)$$
$$= \gamma d + 4c (\leftarrow)$$

For stability

$$\sum F_H = 0, \quad \sum M_C = 0$$

$$\sum F_H = 0$$

$$P_{p1} - P_{p2} - P_{a1} = 0$$

$$(4c - \rho) \times D - \frac{1}{2} (4c + \rho + 4c - \rho) \times \bar{y}$$

$$- P a_1 = 0 \quad \text{--- (1)}$$

$$\Sigma M_c = 0$$

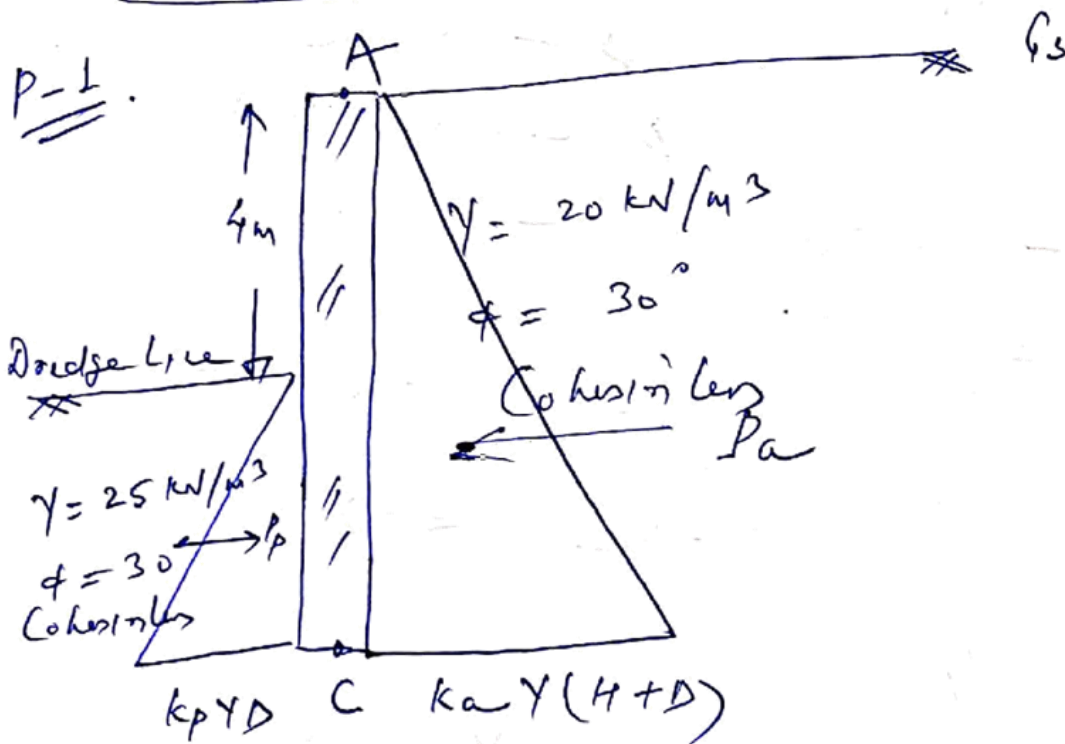
$$(4c - \rho) \times D \times \frac{D}{2} - \frac{1}{2} (4c + \rho + 4c - \rho) \times \bar{y} \times \frac{\bar{y}}{3}$$

$$- P a_1 (D + \bar{z}_1) = 0 \quad \text{--- (2)}$$

Solve eq<sup>n</sup> (1) & (2)

$$D = \sqrt{\quad} \quad \text{and} \quad \bar{y}$$

Provide depth  $\delta = 1.3 D$   
embedment



For Active Condition

$$k_a = \frac{1 - \sin 30}{1 + \sin 30} = \frac{1}{3}$$

$$k_p = \frac{1 + \sin 30}{1 - \sin 30} = 3$$

$$P_a = \frac{1}{2} k_a \gamma (H+D)^2 \rightarrow \text{acting at } \left(\frac{H+D}{3}\right) \text{ from base.} \quad (6)$$

$$= \frac{1}{2} \times \frac{1}{3} \times 20 (H+D)^2$$

$$P_a = \frac{20}{6} (H+D)^2 \text{ acting at } \left(\frac{H+D}{3}\right)$$

$$P_p = \frac{1}{2} k_p \gamma D^2 \text{ acting at } \frac{D}{3} \text{ from base}$$

$$= \frac{1}{2} \times 3 \times 25 \times D^2 \text{ acting at } \frac{D}{3} \text{ from base}$$

$$= \frac{75}{2} D^2 \text{ acting at } \frac{D}{3} \text{ from base}$$

$$\sum M_c = 0$$

$$P_a \times \left(\frac{H+D}{3}\right) - P_p \times \frac{D}{3} = 0$$

$$\Rightarrow \frac{20}{6} (H+D)^2 \times \frac{(H+D)}{3} = \frac{75}{2} D^2 \times \frac{D}{3}$$

$$\Rightarrow \frac{10}{3} (H+D)^3 = 37.5 D^3$$

$$\Rightarrow 3.33 (H+D)^3 = 37.5 D^3$$

$$D = 3.22 \text{ m}$$

Factor of Safety is not given in the problem, so increase the value of  $D$  by 30%.

$$\text{Depth of embedment} = 1.3 D = 1.3 \times 3.22 = 4.2 \text{ m}$$